

TODAY'S DATE:

11/25/19

Homework

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Learning Target: I can solve a system of equations using the substitution method.

Warm Up: Is $(5, 8)$ a solution to the following equation: $y = 2x + 1$

ordered pair,
- coordinate
 (x, y)

$$8 = 2(5) + 1$$

$$8 \neq 11$$

Not a solution!

Guided Practice: Solving a system of equations by substitution

Important: to use substitution method, one equation must be in the form $y =$ or $x =$

Exercise 1: Solve the following system of equations-

$$y = 2x - 3$$

$$y = -2x + 5$$

Step 1: Substitute the $x =$ or the $y =$ expression into the other equation.

$$2x - 3 = -2x + 5$$

$$+2x \quad +2x$$

Step 2: Now that you have one equation with one variable, you can solve for that variable.

$$4x - 3 = 5$$

$$+3 \quad +3$$

$$4x = 8$$

$$\div 4 \quad \div 4$$

$$x = 2$$

$$y = 2x - 3$$

$$y = 2(2) - 3$$

$$y = 1$$

Step 3: To find the second variable, substitute the first value that was found into the one of the original equations. Then solve for the other variable.

Solution: $(2, 1)$
x, y

Step 4: CHECK! (2 equations means 2 checks)

Check:

① $y = 2x - 3$
 $1 = 2(2) - 3$
 $1 = 1$
✓

② $y = -2x + 5$
 $1 = -2(2) + 5$
 $1 = 1$
✓

Exercise 2- Solve the system algebraically by the substitution method.

$$\begin{cases} 3x + y = -24 \\ x = y + 4 \end{cases}$$

$3(y+4) + y = -24$
 $3y + 12 + y = -24$
 $4y + 12 = -24$
 $\begin{array}{r} 4y + 12 = -24 \\ -12 \quad -12 \\ \hline 4y = -36 \\ \hline y = -9 \end{array}$
 \therefore
 $x = y + 4$
 $x = -9 + 4$
 $x = -5$

Solution
 $(-5, -9)$

Check

Check $(-5, -9)$

$$\begin{aligned} 3(-5) + (-9) &= -24 \\ -15 - 9 &= -24 \\ -24 &= -24 \\ \checkmark \end{aligned}$$

$$\begin{aligned} -5 &= -9 + 4 \\ -5 &= -5 \\ \checkmark \end{aligned}$$

Exercise 3- Solve the system algebraically by the substitution method.

$$\begin{cases} 2x + 4y = 16 \\ y = 2x - 6 \end{cases}$$

$2x + 4(2x - 6) = 16$
 $2x + 8x - 24 = 16$
 $10x - 24 = 16$
 $\begin{array}{r|l} 10x - 24 & = 16 \\ +24 & +24 \\ \hline 10x & 40 \\ \hline 10 & 10 \\ \hline x & = 4 \end{array}$
 $y = 2(4) - 6$
 $y = 8 - 6$
 $y = 2$

Solution
 $(4, 2)$

Check

$$\begin{aligned} 2x + 4y &= 16 \\ 2(4) + 4(2) &= 16 \\ 8 + 8 &= 16 \\ 16 &= 16 \\ \checkmark \end{aligned}$$

$$\begin{aligned} y &= 2x - 6 \\ 2 &= 2(4) - 6 \\ 2 &= 8 - 6 \\ 2 &= 2 \\ \checkmark \end{aligned}$$

Problem Set: Solve each of the systems below by the substitution method. Check your solution

1) $y = 2x - 3$
 $y = -3x + 2$

Check

2) $y = x - 2$
 $2x + 2y = 4$

Check