

## 9-1: Converse of the Pythagorean Theorem

"I can use the Pythagorean Theorem to determine if a triangle is a right triangle."

The Pythagorean Theorem states that in a right triangle, the sum of the squares of the lengths of the legs is equal to the square of the length of the hypotenuse.

$$\text{Leg} \quad a^2 + b^2 = c^2 \quad \text{Hypotenuse}$$

$\underbrace{\hspace{1.5cm}}_{a+b}$ 
 $\underbrace{\hspace{1.5cm}}_c$

$\underbrace{\hspace{1.5cm}}_{\text{Leg}}$ 
 $\underbrace{\hspace{1.5cm}}_{\text{Leg}}$

- A Pythagorean Triple is a set of 3 positive integers that satisfy the Pythagorean Theorem.
- The converse of the Pythagorean Theorem states that IF the Pythagorean Theorem is true for the side lengths of a triangle, then it MUST be a RIGHT triangle.
- Remember: the two shorter sides are the legs, a and b.
- The longest side is called the hypotenuse, c.

Determine whether each triangle is a right triangle or not. Show all work, including formulas and substitutions.

<p>1) 3, 5, 6<sup>c</sup></p> <p><b>NO</b></p> $a^2 + b^2 = c^2$ $3^2 + 5^2 = 6^2$ $9 + 25 = 36$ $34 \neq 36$	<p>2) 36, 77, 85<sup>c</sup></p> <p><b>Yes</b></p> $a^2 + b^2 = c^2$ $36^2 + 77^2 = 85^2$ $1296 + 5929 = 7225$ $7225 = 7225$
<p>3) 18, 80, 81<sup>c</sup></p> <p><b>NO</b></p> $a^2 + b^2 = c^2$ $18^2 + 80^2 = 81^2$ $324 + 6400 = 6561$ $6724 \neq 6561$	<p>4) 0.9, 1.2, 1.5<sup>c</sup></p> <p><b>Yes</b></p> $a^2 + b^2 = c^2$ $0.9^2 + 1.2^2 = 1.5^2$ $0.81 + 1.44 = 2.25$ $2.25 = 2.25$

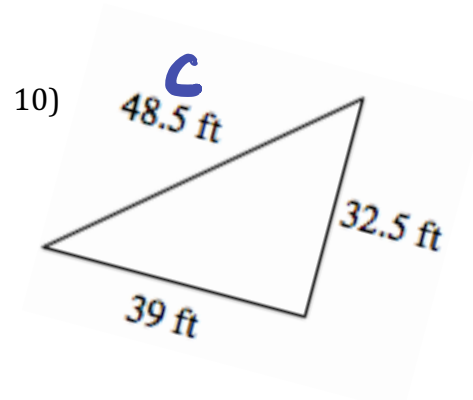
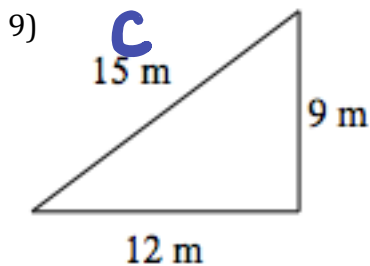
**Problem Set: Determine whether each triangle is or is not a right triangle. Show all work including formulas and substitutions.**

5) 20, 21, 29 <sup>C</sup>

6) 15, 24, 25

7) 3.6, 4.8, 6.2

8) 9, 41, 40

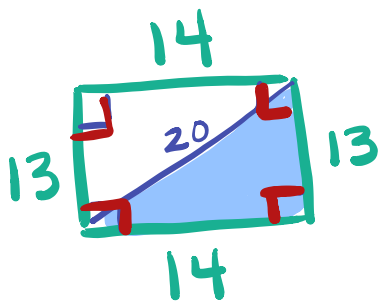


11) If 6-8-10 is a Pythagorean Triple, find 3 more similar Pythagorean Triples.  
<sup>x2</sup> ↘

3-4-5 \* Any multiple is also triple.

12, 16, 20      18, 24, 30      30, 40, 50  
 9, 12, 15      60, 80, 100

12) Mr. Winston is adding a sunroom to his house. After laying the foundation and building the frame he double checks his measurements. Mr. Winston found that his 14 ft. by 13 ft. (rectangular) sunroom had a diagonal measurement of 20 ft. Why is Mr. Winston in trouble?



$$13^2 + 14^2 = 20^2$$

$$169 + 196 = 400$$

$$365 \neq 400$$

Not a right angle → rectangle.