Unit 1: Building Blocks of Algebra

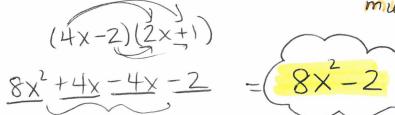
- Number Properties (Distributive, Commutative, Associative, Additive, Multiplicative)
- Distributive Property & DOUBLE Distributing
- **1.** While solving the equation $\frac{4(x+2)}{2} = 28$, Jim wrote $\frac{4x+8}{2} = 28$. Which property did he use?
 - (1) Distributive
- (2) Associative
- (3) Commutative
- (4) Identity

- multiplied by 4 to eliminate (). 2. When solving the equation $4(3x^2 + 2) 9 = 8x^2 + 7$, Emily wrote $4(3x^2 + 2) = 8x^2 + 16$ as her first step. Which property justifies Emily's first step?
 - (1) Addition property of equality
 - [2] Commutative property of addition
 - (3) Multiplicative property of equality
 - (4) Distributive property of multiplication
- $4(3x^2+2)-9=8x^2+7$ +9 $= 8x^2+16$ $= 8x^2+16$ $= 8x^2+16$
- **3.** Jonah was asked to solve the equation: 3x 5 = 16. Which of the number properties will he have to apply to find the solution?
 - ✓ i. Additive Property of Equality
 - ✓ ii. Multiplicative Property of Equality
 - Distributive Property iii.
 - **Commutative Property** iv.
 - (2) i and ii
 - (3) i, ii, and iii
 - (4) i and iv

X = 7

- multiply 4. What is the product of (c + 8) and (c - 5)?
 - (1) c² + 3c 40 (2) c² 3c 40
 - $(3) c^2 + 13c 40$
 - $(4) c^2 40$

- 5. What is the product of (3x + 2) and (x 7)?
 - 3x2-21x+2x-14 = (3x2-19x-14)
- 6. Fred is given a rectangular picture frame as a birthday gift. If the length of the frame is represented by 4x - 2 and the width of the frame is represented by 2x + 1, find the area of the picture frame in square inches. multiply



Unit 2: Linear Expressions, Equations, & Inequalities

Don't Call Me After Midnight

7. What is the value of x in the equation

$$4x - 3 = 5?$$
 $+3 + 3$
 $+4 \times 8$
 $+ \times 8$

9. What is the value of x in the equation 13x - 2(x + 4) = 8x + 1?

8. What is the value of x in the equation

$$5(2x-7) = 15x-10?$$

$$10x-35 = 15x-10$$

$$-10x$$

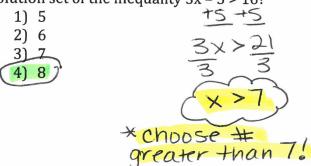
$$-35 = 5x-10$$

$$+10$$

$$-25 = 5x$$

$$5$$

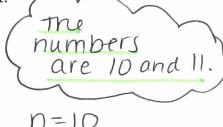
10. Which of the following integers is in the solution set of the inequality 3x - 5 > 16?



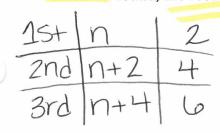
- 11. Convert each into algebraic equations:
 - 1) Twice a number is eight less than four times that number. $2 \times = 4 \times -8$
 - 2) Four times the sum of a number and two is twenty. +(n+2) = 20
 - 3) Nine less than twice a number is four times the sum of the number and five. 2n-9=4(n+5)
- 12. Find two consecutive integers such that the sum of the integers equals 21.

$$(n)+(n+1)=21$$

 $2n+1=21$
 $2n=20$



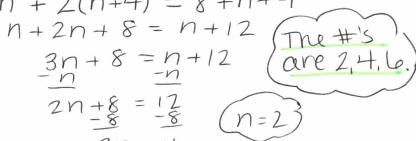
13. Three consecutive even integers have the property that when the sum of the first integer and twice the second is found, the result is eight more than the third. What is the largest integer?



$$n + 2(n+4) = 8+n+4$$

 $n + 2n + 8 = n + 12$

$$3n + 8 = n + 12$$



$$2n + 8 = 12$$

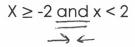
 -8
 -9
 -9
 -9

$$(n=2)$$

14. Graph the solution on a number line:



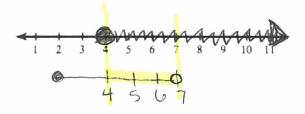






15. Solve algebraically:
$$4(3x-5)+7 \ge 8x+3$$
 $12x-20+7 \ge 8x+3$
 $12x-13 \ge 8x+3$
 $-8x$
 $-8x$
 $-8x$
 $-8x$
 $-12x-13 \ge 8x+3$
 $-12x$

Graph the solution on the number line below:



Write in Interval Notation: (4,00)

[Included]

(not included)

If x is a number in the interval [2, 7] state all integers that satisfy the given inequality above.

Unit 3: Functions

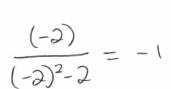
16. Which relation is NOT a function?

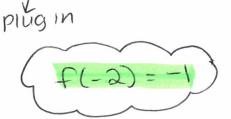
- 1) {(1, 5), (2, 6), (3, 6), (4, 7)}

2) {(-1, 6), (1, 3), (2, 5), (1, 7)} The input "1" has two outputs.

 $3) \{(-1, 2), (0, 5), (5, 0), (2, -1)\}$

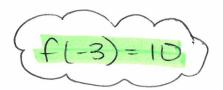
17. If $f(x) = \frac{x}{x^2-2}$, then what is the value of f(-2)?





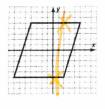
18. If $f(x) = 2x^2 + 3x + 1$ then find the output of f(-3).

$$2(-3)^{2}+3(-3)+1=10$$

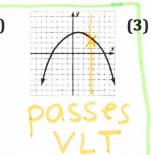


19. Which of the graphs below represents a function?

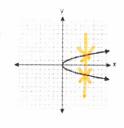
(1)



(2)



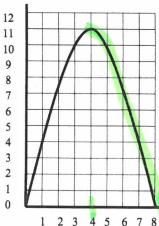




20. The graph to the right represents the height, y, of the ball from the ground after x seconds. For which interval is the ball's height always decreasing?



(2) 4 < x < 8 \(decreasing \) between 4 and 8.



(4) $0 \le x \le 11$

Time (in seconds)

Set	Description	
Natural	{ 1, 2, 3, 4,} the counting numbers	
Whole	{ 0, 1, 2, 3, 4,} the counting numbers plus zero	
Integers	{, -3, -2, -1, 0, 1, 2, 3,} positive and negative WHOLE numbers	
Rational	All numbers that can be written as a fraction (includes terminating and repeating decimals)	
Irrational	Imperfect squares, pi, non-repeating and non-terminating decimals. These numbers cannot be written as a fraction	
Real	All numbers included in rational and irrational numbers	

21. Which domain would be the *most appropriate* set to use for a function that predicts the number of household online-devices in terms of the number of people in the household? can't be negative or decimal.

Week

Pay

\$140

\$145

\$152

\$158

average rate of change =
$$\frac{\text{change in } y}{\text{change in } x} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x} = m = SLOPE$$

22. What is the average rate of change of the line that passes through (4, -8) and (2, 6)? \times , \vee , \times 2 \vee 2

$$\frac{6 - 8}{2 - 4} = \frac{14}{-2} = \boxed{7}$$

23. Dan took a summer job, for five weeks, where he received a weekly salary plus tips. His take-home pay is recorded in the table at the right. What was the average rate of change in his weekly take-home pay from week 1 to week 4 of his job?

$$\frac{158 - 140}{4 - 1} = \frac{18}{3} = \frac{\$ \text{ (a per week)}}{-\frac{2}{3}}$$

24. A car is traveling along a straight road. After one hour, the car is 72 miles from New York. After three hours, the car is 188 miles from New York. Determine the average rate the car is traveling.

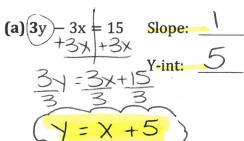
$$(1,72) \qquad 188-72 = 116 = 58 \text{ miles}$$

$$(3,188) \qquad 3-1 = 2 = 58 \text{ miles}$$

Unit 4: Linear Functions



25. Rearrange each of the following equations into y=mx+b form & identify the slope & y-intercept.



(b) $6x - 4y = -20$	Slope: 2
	O Y-int: 5
-4 -4 -4	4
Y=3x+	5)

riting Equations in Slope-Intercept Form

Step 1: Take two points and find the slope

Step 2: Pick one of the given coordinates

Step 3: Substitute the slope (m), x, and y into y = mx + b

Step 4: Solve for the y-intercept (b)

Step 5: Substitute the slope (m) and the y-intercept (b) into y = mx + b

26. Water is draining out of a bathtub such that the volume still left, g-gallons, is shown as a function of the number of minutes, m, it has been draining.

<i>m</i> , minutes	1	2	3	4	5
g(m), gallons	24	21	18	15	12
gallons					

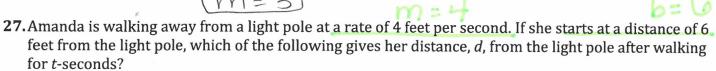
Assuming that the relationship is linear, create an equation that represents the table above.

$$(1,24)$$

$$(2,21)$$

$$M = \frac{24-21}{2-1} = \frac{3}{1}$$

$$M = 3$$



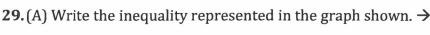
(1)
$$d = 4t + 6$$

(3)
$$d = 6t + 4$$

$$(2) \ d = \frac{3}{2}t$$

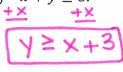
(4)
$$d = -6t + 4$$

- 28. A television company charges a one-time installation fee and a monthly service charge. The total cost is modeled by the function y = 40 + 90x. Which statement represents the meaning of each part of the function?
 - 1) y is the total cost, x is the number of months of service, \$90 is the installation fee, and \$40 is the service charge per month
 - 2) y is the total cost, x is the number of months of service, \$40 is the installation fee, and \$90 is the service charge per month.
 - 3) x is the total cost, y is the number of months of service, \$40 is the installation fee, and \$90 is the service charge per month.
 - 4) x is the total cost, y is the number of months of service, \$90 is the installation fee, and \$40 is the service charge per month.

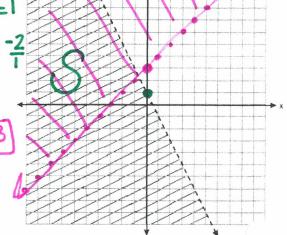




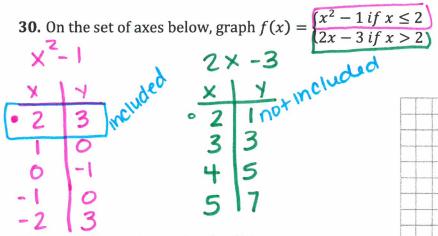
(B) On the same set of axes, graph the inequality $-x + y \ge 3$.



(C) State one point that is in the solution set. (-3,3)

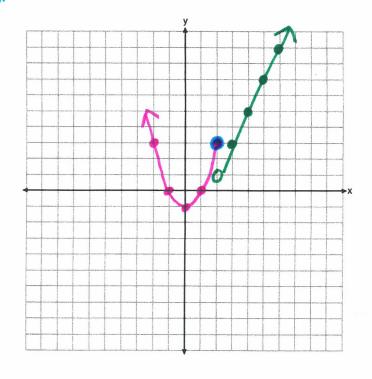


30. On the set of axes below, graph
$$f(x) = \begin{cases} x^2 - 1 & \text{if } x \le 2 \\ 2x - 3 & \text{if } x > 2 \end{cases}$$



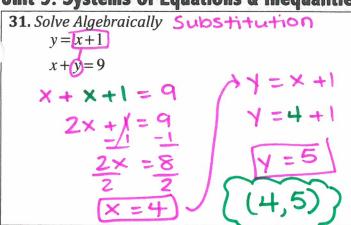
Determine the output value for f(2).

$$f(2)=3$$



Unit 5: Systems of Equations & Inequalities

Elimination.



32. Solve Algebraically
$$-3(2x+3y=6) - 6x - 9y = -18$$

$$2(3x+5y=15) + 6x + 10y = 30$$

$$2x + 3(12) = 6$$

$$2x + 3(2) = 6$$

$$2x + 3(3) = 6$$

$$2x = -36$$

9b+10h ≥ 200

x - y = 3

$$2x - 3y = -1$$

A)
$$-2x-2y=-6$$
 B) $-2x+2y=3$
 $2x-3y=-1$

B)
$$-2x + 2y = 3$$

C)
$$2x - 2y = 6$$
 (x2)
 $2x - 3y = -1$

D)
$$3x + 3y = 9$$

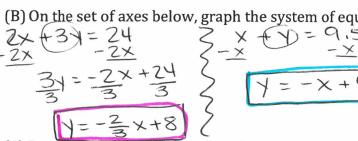
 $2x - 3y = -1$

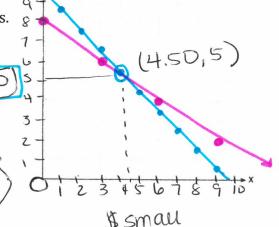
厂\$7

- **34.** Gavin works for a restaurant during the weekends. He is paid \$9 per hour for bussing and \$10 per hour for hosting. He can work a maximum of 20 hours per week and he wants to earn at least \$200 this weekend. If b represents the hours spent bussing and h represents the hours spent hosting, write a system of inequalities can be used to represent these conditions. hours b+h \ 20
- 35. Christian and Shannon are selling candles for a school fundraiser. Customers can buy small candles and large candles. After the first week, Christian sold 2 small candles and 3 large candles for \$24. Shannon, on the other hand, sold 1 small candle and 1 large candle for \$9.50.
 - (A) Write a system of equations that describes the given situation. Let x represent the cost of each small candle and y represent the cost of each large candle.

$$2x + 3y = 24$$
 $1x + 1y = 9.50$

(B) On the set of axes below, graph the system of equations. §





(C) Determine the cost of one small candle and the cost of one large candle. Smail = \$4.50 2/X+3/=24

large = \$5

Directions: Choose the best answer. Answer ALL questions. Show ALL work in column 2. If there is no mathematical work to be shown, write an explanation or definition to support your answer!

1. If $A = \frac{2}{3}(B+8)$, then B i	s equivalent to
---	-----------------

(1)
$$\frac{3}{2}A + 8$$

(1)
$$\frac{3}{2}A + 8$$
 (2) $\frac{3}{2}A - 8$

(3)
$$\frac{2}{3}A + 8$$
 (4) $\frac{2}{3}A - 8$

$$(4) \ \frac{2}{3}A - 8$$

Show steps to get B alone:

$$A = \frac{2}{3}(B+8)$$

$$\frac{3}{2}A = B + 8$$

2. If the domain of
$$f(x) = 2x + 1$$
 is $-2 \le x \le 3$, state the range of this function.

Support with a table: • Put
$$f(x) = 2x+1$$

$$X = \text{input (domain)}$$
 $Y = \text{output (range)}$
3. If $f(x) = 3^x \text{ and } g(x) = 2x + 4$, at which value of x is

$$f(x) \le g(x)?$$

- (1) 4
- (2) 3
- (3) 2
- (4) 1

$$f(x)=3^{x}$$

$$\begin{vmatrix} 2 & 2/5 & 10 \\ 9 & 9 & 8 \\ 13 & 6 & 6 \end{vmatrix}$$

9(x) = 2x + 4

4. Which expression can be used to change 75 kilometers per hour to meters per minute?

1)
$$\frac{\text{not diagonal}}{1 \text{ hr}} \times \frac{1 \text{ km}}{1,000 \text{ m}} \times \frac{1 \text{ hr}}{60 \text{ min}}$$
 3) $\frac{75 \text{ km}}{1 \text{ hr}} \times \frac{1,000 \text{ m}}{1 \text{ km}} \times \frac{1 \text{ hr}}{60 \text{ min}}$

2)
$$\frac{75 \text{ km}}{1 \text{ hr}} \times \frac{1 \text{ km}}{1,000 \text{ m}} \times \frac{60 \text{ min}}{1 \text{ hr}}$$
 4) $\frac{75 \text{ km}}{1 \text{ hr}} \times \frac{1,000 \text{ m}}{1 \text{ km}} \times \frac{60 \text{ min}}{1 \text{ hr}}$

not diagonal

Look for units that are the same diagonally that you can cross out.

5. What is the average rate of change of the line	Label points with (x,y)			
that passes through the points (4,-8) and (2,6)?	Average rate of change Av-v-v			
$(1) - \frac{1}{7}$ $(2) \frac{1}{7}$	Average rate of change $\Delta y = \frac{y_z - y_i}{\Delta x}$ (Slope)			
(3) 7	-8-6-7			
resignation of page 1 people				
	4-2			
6. If h represents a number, which equation is a	1			
correct translation of "Sixty more than 9 times a number is 375"?	Choice 1 never mentions 60.			
variable = turn around	Choice 3 subtracts, more than means add			
(1) $9h = 375$	Choice 4 multiplies 60 and h.			
$\begin{array}{c} (1) & 9h = 375 \\ (2) & 9h + 60 = 375 \end{array}$	Chota			
(3) $9h - 60 = 375$				
(4) 60h + 9 = 375				
7. If $f(x) = \frac{x}{x^3 - 2}$, what is the value of $f(-2)$?	put function into calculator (4=)			
$(1) - \frac{1}{5}$ $(2) - \frac{1}{3}$	look for output of (-2)			
(3) $\frac{1}{3}$ (4) $\frac{1}{5}$	$-\Delta 1.4$			
(3) $\frac{3}{3}$ (4) $\frac{5}{5}$	$-2\frac{7}{5}$			
	,			
8. What is the slope of a line represented by the equation $2y = x - 4$	Is it in slope intercept form (y=mx+b)?			
equation 2y = x = 4	* No it isn't y is not alone!			
(1) 1 (2) $\frac{1}{2}$				
2	$\frac{2}{2}y = \frac{x}{2} - \frac{4}{2}$			
(3) -1 (4) $-\frac{1}{2}$	$y = \frac{x}{2} - 2$ put in your sneaky			
	$y = \frac{1}{2} \times -2$			
	Y-intercept			
O What is a solution to the in-smaller	Slope y micrepi			
9. What is a solution to the inequality $-6x - 17 \ge 8x + 25$?	-6 x-17 ≥ 8x+25 (The sign			
	+17			
(1) -3	$\frac{-6x \ge 8/x + 42}{-6x \ge 8/x + 42}$ (because you)			
(2) 3 (3) -4	-6x \ge 8x + 42 \text{because you} \\ -8x \text{6 divide by a}			
(4) 4	Vy negative			
	-14× ≥ 42 × (≤)-3			
10. Which relation is <u>not</u> a function?				
x y x y x y x y	X's can not repeat			
(1) $\{(1,5),(2,6),(3,6),(4,7)\}$	Label your points with(x,y)			
(2) $\{(4,7),(2,1),(-3,6),(3,4)\}$ (3) $\{(-1,6),(1,3),(2,5),(1,7)\}$				
$(4) \{(-1,2),(0,5),(5,0),(2,-1)\}$				

Algebra 1 CC Midterm R

Directions: Choose the best answer. Answer ALL questions. Show ALL work in column 2. If there is no mathematical work to be shown, write an explanation or definition to support your answer!

- 1) When solving the equation $4(3x^2 + 2) 9 = 8x^2 + 7$, Emily wrote $4(3x^2 + 2) = 8x^2 + 16$ as her first step. Which property justifies Emily's first step?
- (1) addition property of equality
- 2) commutative property of addition
- multiplication property of equality
- distributive property of multiplication over addition
- 2) The ages of three brothers are consecutive even integers. Three times the age of the youngest brother exceeds the oldest brother's age by 48 years. What is the age of the youngest brother?
- 14 1)
- 2) 18
- 22 3)
- (4) 26

- addition property of equality add opposite or inverse to cancel.
- commutative property order changes without outcome changing
- multiplicative property of equating-multiply by reciprocal to cancel.
- distribution property multiply by number outside parentneses.
- Make a table Write your Let statement & Equation here
- $X = \begin{cases} 1^{st} \cos s \cdot e^{yen} # \end{cases}$ (youngest) = oldest + 48 $X+Z = 2^{rd} \cos s \cdot e^{yen} # \end{cases}$ $(3 \times 2^{rd} + 4 \times 4) = 0$
- X+4 3rd cons. even# (30
- The youngest brother is 26 $\frac{2x}{3} = \frac{52}{3} = \frac{x}{26}$ brother is 26
- 3) Write the three ways to express the inequality represented in the accompanying graph?

- Interval Notation: (-3, 4]
- Single Inequality: $3 < x \le 4$
- Compound Inequality X > -3 and $X \le 4$ (Connect with and or or)
- 4) Julia went to the movies and bought one jumbo popcorn and two chocolate chip cookies for \$5.00. Marvin went to the same movie and bought one jumbo popcorn and four chocolate chip cookies for \$6.00. Write the system of equations. Do Not Solve. I means more than one
 - equation
- Let p = cost of popcorn C = cost of choc. cookies
 - 1p+2c=5.00 1p + 4c = 6.00
- 5) Ryan can sell no more than 400 raffle tickets for a school fundraiser. His goal is to make at least of \$1200 in sales. To win Beats headphones, you must purchase a 15 red ticket. To win an Kindle, you must purchase a \$2 blue ticket. If(r) represents the number of red tickets and brepresents the number of blue tickets, which system of inequalities represents this situation?
- Annotate to justify you answer choice.

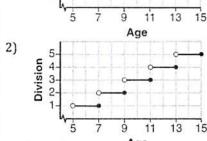
no more than
$$\leq$$
 at least \geq

- (1) $r + b \ge 400$ and $5r + 2b \le 1200$
- (2) $r + b \le 400$ and 5r + 2b > 1200
- (3) r + b > 400 and 5r + 2b > 1200
- (4) $r + b \le 400$ and $5r + 2b \le 1200$

6) Vince can start wrestling at age 5 in Division 1. He remains in that division until his next odd birthday when he is required to move up to the next division level. Which graph correctly represents this information?

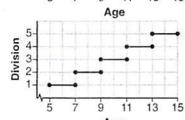
(1)Division

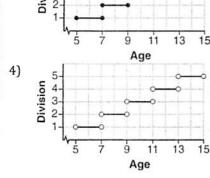
Step Functions O circle not Included allows us to pass through



3)

@ circle, included you can not pass through





7) Harry has a data plan that costs \$10.95 per month plus \$.25. per gigabyte he uses. Nicole has a data plan that costs \$12.45 per month plus \$.15 per gigabyte she uses. For what number of gigabytes do the two plans cost the same?

means to q = # of gigabytes set equal to each other Harry 10.95 + .259 Nicole 12.45 + .159

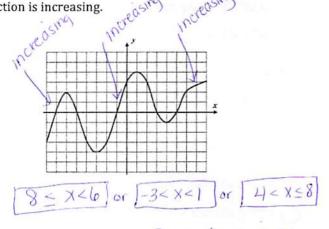
$$\begin{array}{r}
 10.95 + .259 &= 12.45 + .159 \\
 -10.95 &= 10.95
 \end{array}$$

$$\begin{array}{r}
 .2.59 &= 1.50 + .159 \\
 -.159 &= .159
 \end{array}$$

$$\begin{array}{r}
 .109 &= 1.50 \\
 .10 &= .15
 \end{array}$$

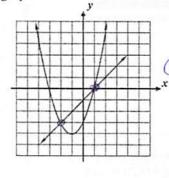
At 15 gigabytes the plans will cost the same,

8) Using the graph below, state an interval at which the function is increasing.



#'s come from domain or X-axis

9) The quadratic function, f(x) and the linear function g(x) are graphed below. For what values of x does f(x)=g(x)?



(1,0) and (-2,-3)

or {-2,13

Look for where the functions intersect each other.

Inequality symbols always go in the same direction

Algebra 1 CC Midterm Review Homework #3

Directions: Choose the best answer. Answer ALL questions. Show ALL work in column 2. If there is no mathematical work to be shown, write an explanation or definition to support your answer!

1. A system of equations are given below.

$$x + 2y = 5$$

$$2x + y = 4$$

Which system of equations does not have the same solution?

$$(1) 3x + 6y = 15 2x + y = 4$$

$$(1)$$
 $3x + 6y = 15$ (2) $4x + 8y = 20$ $2x + y = 4$ $2x + y = 4$

$$\sqrt{3}$$
 $x + 2y = 5$
 $6x + 3y = 12$

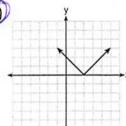
$$\begin{array}{c} \times 4 \\ \times 4 \\ \times 4x + 2y = 5 \\ \times 4x + 2y = 12 \end{array}$$

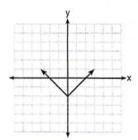
Use elimination method or MATRIX

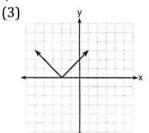
$$\begin{bmatrix} 1 & 2 & 5 \\ 2 & 1 & 4 \end{bmatrix} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 2 \end{bmatrix} (1,2)$$

2. Which graph represents the equation y = |x - 2|?



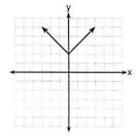






(4)

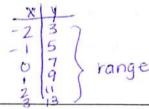
center



(Graph)

3. Consider the function given by f(x) = 2x + 7. Find its range over the domain interval -2 < x < 3.

 $f(x) = 2x + 7 \leftarrow put in calculator + get a table$



4. Officials in a town use a function, C, to analyze traffic patterns. C(n) represents the rate of traffic through an intersection where *n* is the number of observed vehicles in a specified time interval. What would be the most appropriate domain for the function?

(1)
$$\{...-2, -1, 0, 1, 2, 3, ...\}$$
 (3) $\{0, \frac{1}{2}, 1, 1\frac{1}{2}, 2, 2\frac{1}{2}\}$ (2) $\{-2, -1, 0, 1, 2, 3\}$ (4) $\{0, 1, 2, 3, ...\}$

If n represents the number observed vehicles going through an intersection the only domain would be #4. You can not have negative rehicles or Fractions of vehicles.

5. Over which interval is the function to the right

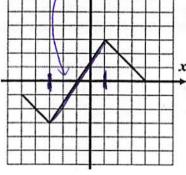
increasing?

(1)
$$-1 < x < 4$$

(2)
$$-3 < x < 3$$

$$(3)$$
 -3 < x < 1

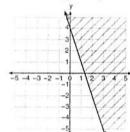
(4)
$$1 < x < 4$$



- 6. A water tank is being drained by a pump at a constant rate. The volume in the tank, V, in gallons, is given by the equation: V(t) = -4t + 280, where t is the time, in minutes, the pump has been on. Based on this equation, which statement is true?
 - (1) The tank lost 280 gallons after 4 minutes of draining.
 - (2) The water tank started with 280 gallons and is draining at a rate of 4 gallons per minute.
 - (3) The water tank is being filled at a rate of 4 gallons per minute until it reaches 280 gallons.
 - (4) The water tank started with 280 gallons and is filling at a rate of 4 gallons per minute.

rate of change 7 start, beginning (slope) $y = m \times + b$ (y-intercept)

7. Which inequality is represented in the graph below?



$$(1) y \ge -3x + 4$$

(2)
$$y \le -3x + 4$$

(3)
$$y \ge -4x - 3$$

(4)
$$y \le -4x - 3$$

solid line indicates Symbol must be ≤ or ≥

y-intercept is 4 which rules out choice 3 and 4.

The inequality is shaded upwards Indicating >

8. Which value of x is in the solution set to the system of equations below?

$$9x + 6y = 36$$

$$10x - 4y = 8$$

Use elimination method or matrix

Because it is asking for the value of X, the answer is 2

9. Create an algebraic equation for the following statement, then determine the value of the number.

Three times the sum of a number and six is equal to twelve less than that number.

$$3(n+6) = n-12$$

Annotate 2 operations (+) means you need parentheses.

less than is a turn around word.